

Exploring Serial NHG with Eastern Andalusian Harmony

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- Noisy Harmonic Grammar: probabilistic implementations of Harmonic Grammar (Jesney 2007; Hayes 2017; Flemming 2017; Zuraw & Hayes 2017).
- Only one member of this family supports an analysis of optionality in Eastern Andalusian Harmony (Kaplan 2018a; Kaplan 2019).
- The harmony-driving constraint in this analysis requires serialism.

A crucial, unaddressed question

How does serial Noisy Harmonic Grammar work?

Eastern Andalusian Harmony

- Jiménez & Lloret (2007); Lloret & Jiménez (2009); Lloret (2018)
- /s/-aspiration (= deletion) causes laxing of word final vowel, which triggers [-ATR] harmony on the stressed syllable:

<i>tesis</i>	'tɛsɪ	'thesis'	<i>nenes</i>	'nɛnɛ	'babies'
<i>tiens</i>	'tjɛnɛ	'you have'	<i>pesos</i>	'pɛsɔ	'weights'
<i>monos</i>	'mɔnɔ	'monkeys'	<i>lejos</i>	'lɛhɔ	'far'
<i>bocas</i>	'ɔkæ	'mouths'	<i>asas</i>	'asæ	'handles'

- Harmony on other vowels is optional. . .

Eastern Andalusian Harmony

- Nonfinal post-tonic vowels optionally harmonize in lockstep:

treboles 'trɛβolɛ ~ 'trɛβɔɛ 'clovers'
cómetelos 'kɔmetelɔ ~ 'kɔmɛtɛɔ 'eat them (for you)!'
 *'kɔmɛtelɔ, *'kɔmetɛɔ

- Likewise for pretonic vowels; post-tonic harmony is a prerequisite for pretonic harmony:

momentos mo'mɛntɔ ~ mɔ'mɛntɔ 'instants'
relojes re'lɔhɛ ~ rɛ'lɔhɛ 'watches'
monederos mone'ðɛrɔ ~ mɔnɛ'ðɛrɔ 'purses'
 *mɔne'ðɛrɔ, *monɛ'ðɛrɔ
recógelos re'kɔhelɔ ~ re'kɔhɛɔ ~ rɛ'kɔhɛɔ 'pick them'
 *rɛ'kɔhelɔ

Eastern Andalusian Harmony

- But high vowels do not undergo harmony:

<i>crisis</i>	'krisɪ	'crisis'
<i>muchos</i>	'muʃɔ	'many'
<i>ídolos</i>	'iðolɔ ~ 'iðɔlɔ	'idols'
<i>cojines</i>	ko'hinɛ ~ kɔ'hinɛ	'pillows'
<i>cotillones</i>	koti'ʒɔnɛ ~ kɔti'ʒɔnɛ	'cotillions'

- When the stressed vowel is high (e.g. *cojines*), harmony becomes derivationally opaque (Kaplan 2020); not dealt with here.

- Positional Licensing triggers harmony on the stressed syllable (Jiménez & Lloret 2007; Lloret & Jiménez 2009; Lloret 2018; Walker 2011):

/'tesis/	LICENSE([-ATR], $\acute{\sigma}$)	*[-ATR]
a. 'tesI	*!	*
☞ b. 'tɛSI		**

- Optionality: using Partial Orders (Anttila 2007), other constraints trigger or block harmony in other positions.

- Standard Positional Licensing is pathological in HG. A replacement (Kaplan 2018b):

$LICENSE([-ATR], \acute{o})$

Assign +1 for each [-ATR] that coincides with \acute{o} and +1 for each additional syllable that [-ATR] appears in.

- Positive constraints & infinite goodness (Kimper 2011a): epenthesize infinite harmonic vowels to increase LICENSE's reward.
- Serialism's repair: outputs are derived over a series of passes through the grammar, with only one change allowed at a time.
- Epenthesis and harmony occur on separate steps, and there's no motivation for harmony absent epenthesis.

What implementations of serial NHG are possible? Which provide satisfactory accounts of Eastern Andalusian? How does serial NHG compare to parallel NHG?

- What we'll see:
 - Hayes's (2017) "classical NHG" has several possible serial implementations; all account for Eastern Andalusian satisfactorily.
 - Other versions of serial NHG overgenerate.
 - These results match the behavior of parallel NHG.
- Other findings:
 - Our choice of anti-harmony constraint can be crucial in serial NHG.
 - Results aren't affected by whether we treat harmony as a one-step or two-step process.

The Core Constraints

- Positive LICENSE drives harmony, *[-ATR] discourages it.
- CRISPEGE (e.g. Ito & Mester (1999)) discourages pretonic harmony:
 - CRISPEGE([-ATR], $\acute{\sigma}$, L): assign -1 for each syllable to the left of the stressed syllable with which it shares a [-ATR] feature (Kaplan 2018c).

Other constraints, effectively undominated

- MAX(-ATR): don't delete [-ATR]
- ANCHOR-R: ensures a lax final vowel (*[tɛsi])
- *[+hi, -ATR]: prevents high vowels from harmonizing. (Outweighed by MAX(-ATR) because final high vowels lax.)

Add noise to the computation of harmony scores at various levels (Hayes 2017):

/rekóhelos/	LICENSE 11	CRISPEGE 0.25	*[-ATR] 11	<i>H</i>
a. re'kohelɔ			-1	-11
(☞) b. re'kɔhelɔ	+2		-2	0
(☞) c. re'kɔhɛɔ	+3		-3	0
(☞) d. re'kɔhɛɔ	+4	-1	-4	-0.25
e. re'kɔhelɔ	+3	-1	-3	-0.25

NHG: the Mechanics

Add noise to the computation of harmony scores at various levels (Hayes 2017): constraint (“classical NHG”),

/rekóhelos/	LICENSE 11 +.5	CRISPEGE 0.25-.2	*[-ATR] 11 +.3	<i>H</i>	
a. re'kohelɔ			-1	-11	→ -11.3
(☞) b. re'kɔhelɔ	+2		-2	0	→ 0.4
(☞) c. re'kɔhɛɔ	+3		-3	0	→ 0.6
(☞) d. re'kɔhɛɔ	+4	-1	-4	-0.25	→ 0.75
e. re'kɔhelɔ	+3	-1	-3	-0.25	→ 0.55

Add noise to the computation of harmony scores at various levels (Hayes 2017): constraint (“classical NHG”), cell,

/rekóhelos/	LICENSE 11	CRISPEGE 0.25	*[-ATR] 11	<i>H</i>	
a. re'kohelɔ	+9	-8	-1 -5	-11	→ -10.5
(☞) b. re'kɔhelɔ	+2 +5	-7	-2 -5	0	→ 2
(☞) c. re'kɔhɛɪɔ	+3 +0	+6	-3 -9	0	→ 2.7
(☞) d. re'kɔhɛɪɔ	+4 -9	-1 +7	-4 +2	-0.25	→ -5.35
e. re'kɔhelɔ	+3 +2	-1 -2	-3 +6	-0.25	→ -1.25

Add noise to the computation of harmony scores at various levels (Hayes 2017): constraint (“classical NHG”), cell, or candidate.

/rekóhelos/	LICENSE 11	CRISPEGE 0.25	*[-ATR] 11	<i>H</i>	
a. re'kohelɔ			-1	-11 +.4	→ -10.6
(☞) b. re'kɔhelɔ	+2		-2	0 +.2	→ 0.2
(☞) c. re'kɔhɛɪɔ	+3		-3	0 -.8	→ -0.8
(☞) d. re'kɔhɛɪɔ	+4	-1	-4	-0.25 .3	→ -.55
e. re'kɔhelɔ	+3	-1	-3	-0.25 .4	→ 0.65

Only constraint-level noise accounts for Eastern Andalusian in parallel NHG (Kaplan 2018a; Kaplan 2019); that’s where we’ll start with serialism.

Serial Versions of Constraint-Level Noise

- 1 Constant noise: weights are perturbed once at the outset, fixing their values for the whole derivation.

$$\text{Step 1: } w(C) + i$$

$$\text{Step 2: } w(C) + i$$

- 2 Variable Noise: weights are perturbed anew at each step in the derivation.

$$\text{Step 1: } w(C) + i$$

$$\text{Step 2: } w(C) + j$$

- 3 Cumulative variable noise: like variable noise, but the starting point for each step is the perturbed weights from the previous step.

$$\text{Step 1: } w(C) + i$$

$$\text{Step 2: } w(C) + i + j$$

- Existing software (OTsoft (Hayes, Tesar & Zuraw 2013), OT-Help (Staubs et al. 2010), e.g.) doesn't support serial NHG.
- My own implementations, built in R (R Core Team 2020).
Some details:
 - Noise was drawn from a normal distribution with mean of 0 and standard deviation of 1.
 - Negative weights were reverted to 0 (following Hayes (2017)).
 - In the event of tied winners, one is chosen at random.
 - Results from each implementation were aggregated over 10,000 iterations.
 - Weights supplied at the outset.

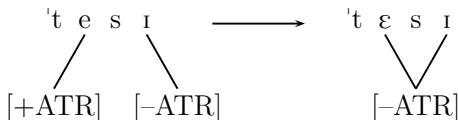
/rekóhelos/	LICENSE 11	CRISPEGE 0.25	*[-ATR] 11
a. re'kohelɔ			-1
(ESP) b. re'kohelɔ	+2		-2
(ESP) c. re'kohelɔ	+3		-3
(ESP) d. re'kohelɔ	+4	-1	-4
e. re'kohelɔ	+3	-1	-3

- Harmony on stressed syllable: $2w(\text{LICENSE}) > w(*[-\text{ATR}])$
- Post-tonic harmony:
 - $w(\text{LICENSE}) > w(*[-\text{ATR}])$ **or**
 - $w(\text{LICENSE}) < w(*[-\text{ATR}])$
- Pretonic Harmony:
 - $w(\text{LICENSE}) > w(*[-\text{ATR}]) + w(\text{CRISPEGE})$ **or**
 - $w(\text{LICENSE}) < w(*[-\text{ATR}]) + w(\text{CRISPEGE})$

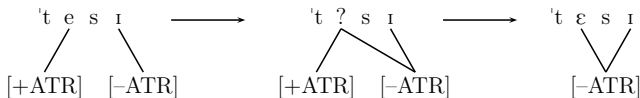
Constraint	Weight
*[-ATR]	11
LICENSE	11
CRISPEdge	0.25
MAX(-ATR)	50
ANCHOR-R	100
*[+hi, -ATR]	40

Representational Assumptions

- Gradualism: one change at a time. What counts as a change?
- ① A vowel harmonizes in one fell swoop:



- ② Harmony is a two-step process (e.g. McCarthy (2008)):



- Fell-swoop harmony for now; revisit this later.

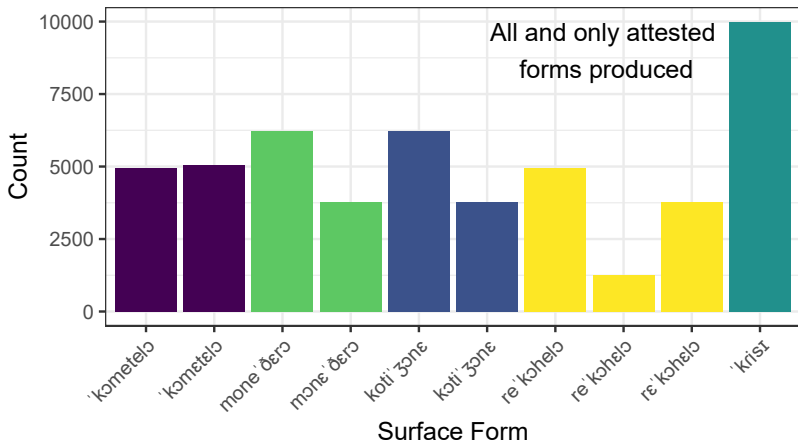
Configurations to Test

- /'kometelos/ 'eat them (for you)!': 2 non-final post-tonic vowels; harmonize both or neither.
- /mone'deros/ 'purses': 2 pretonic vowels; harmonize both or neither.
- /koti'zones/ 'cotillions': high V doesn't stop other pretonic V from optionally harmonizing.
- /re'kohelos/ 'pick them': pretonic V can't harmonize without the post-tonic V.
- /'kɾisis/ 'crisis': 2 high vowels; only licit realization: ['kɾisɪ]

Constant Noise

- Weights perturbed once and for all at the outset.

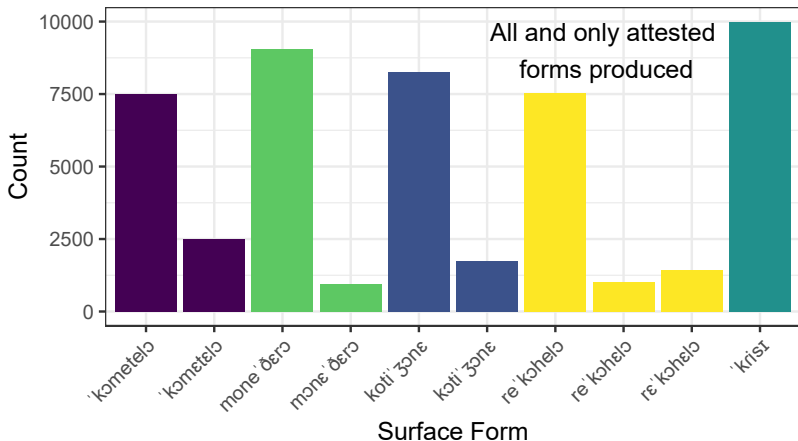
Outputs under Constant Noise



Variable Noise

- New noise on each step.

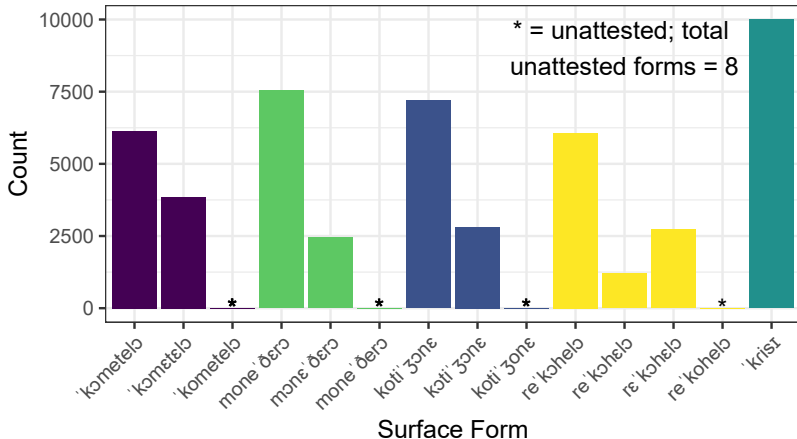
Outputs under Variable Noise



Cumulative Variable Noise

- New noise each step, beginning with previous step's weights.

Outputs under Cumulative Variable Noise



Cumulative Variable Weight

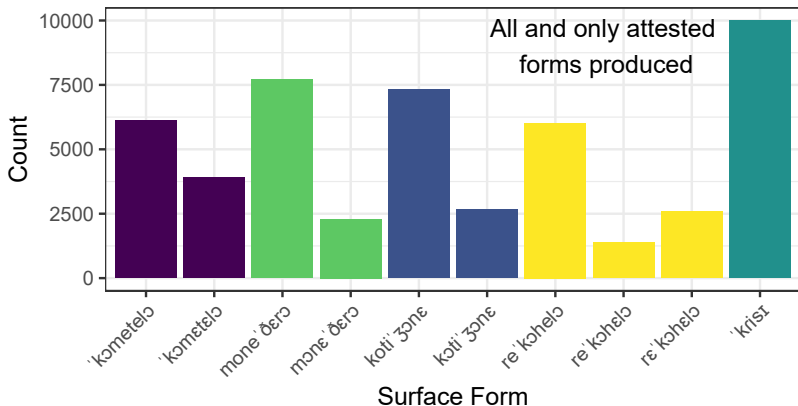
- Bad outcomes result when the accumulation of noise causes a constraint's weight to stray too far.
- E.g. in one derivation yielding *['kometelɔ], LICENSE and *[-ATR]'s final weights are 4.62 and 14.4, respectively. No harmony can happen.
- Cf. constant noise: the greatest such deficit for LICENSE is -4.98 ($w(\text{LICENSE}) = 8.77$; $w(*[-\text{ATR}] = 13.8)$)

Cumulative Variable Weight

- Doubling the weights prevents this:

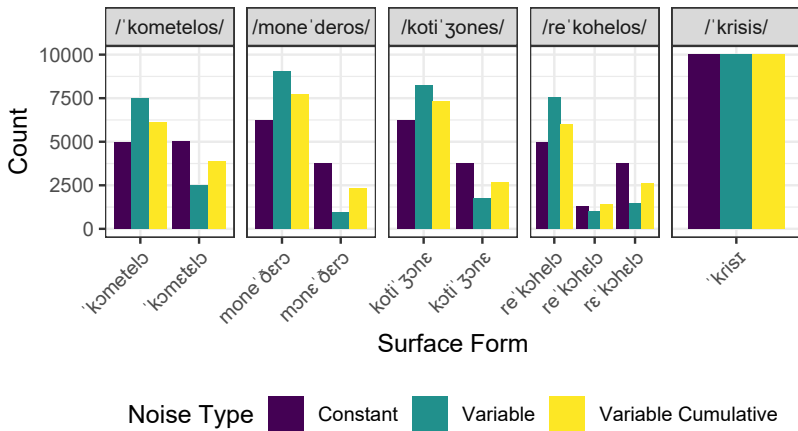
Outputs Using Cumulative Variable Noise

Starting Weights Doubled



Comparison of Frameworks

Surface Form Frequencies with Different Noise Types



- Variable noise makes harmony harder: perturbation must consistently favor harmony.
- Pretonic harmony is rarer than post-tonic harmony (CRISPEGE!).

How Long Until Convergence?

Noise Type	Mean Steps	Maximum Steps
Constant	2.40	4
Variable	3.01	30
Variable Cumulative	2.53	14

- Constant noise: the maximum number of steps is constrained by the number of vowels.
- Variable noise: potential for infinite loop if weights cycle between $w(\text{LICENSE}) > w(*[-\text{ATR}])$ and the reverse.

Constraint-Level Noise: Summary

- All three kinds of constraint-level noise permit accurate models of Eastern Andalusian.
- Cumulative noise is more brittle: weights can stray far from original settings.
- Major differences lie in frequency predictions (which can be adjusted somewhat by changing initial weights), but without frequency data, we can't say which is more accurate.

Candidate- & Cell-Level Noise

- Candidate-level noise: noise added directly to candidates' harmony scores:

/rekóhelos/	LICENSE ₁₁	CRISPEGE _{0.25}	*[-ATR] ₁₁	<i>H</i>	
a. re'kohelo			-1	-11 ₊₄	→ -10.6
(☞) b. re'kohelo	+2		-2	0 ₊₂	→ 0.2
(☞) c. re'kohelo	+3		-3	0 ₋₈	→ -0.8
(☞) d. re'kohelo	+4	-1	-4	-0.25 _{.3}	→ -.55
e. re'kohelo	+3	-1	-3	-0.25 _{.4}	→ 0.65

- Cell-level noise: different noise for each cell in a tableau:

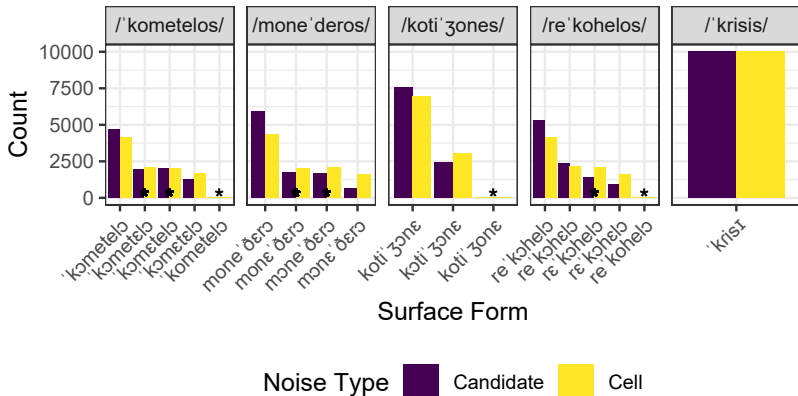
/rekóhelos/	LICENSE ₁₁	CRISPEGE _{0.25}	*[-ATR] ₁₁	<i>H</i>	
a. re'kohelo	+9	-8	-1 _{-.5}	-11	→ -10.5
(☞) b. re'kohelo	+2 ₊₅	-7	-2 _{-.5}	0	→ 2
(☞) c. re'kohelo	+3 ₊₀	+6	-3 _{-.9}	0	→ 2.7
(☞) d. re'kohelo	+4 _{-.9}	-1 ₊₇	-4 ₊₂	-0.25	→ -5.35
e. re'kohelo	+3 ₊₂	-1 _{-.2}	-3 ₊₆	-0.25	→ -1.25

- Weights used:

Constraint	Weight
*[-ATR]	11
LICENSE	11
CRISPEdge	0.25
MAX(-ATR)	50
ANCHOR-R	100
*[+hi, -ATR]	40

Candidate- & Cell-Level Noise

Candidate- and Cell-Level Noise



* = unattested; those with near-zero frequencies (6 tokens) all come from cell-level noise.

- It is impossible for $*[mone'dero]/*[mone'dero]$ to be less frequent than both $[mone'dero]$ and $[mone'dero]$.

Candidate- & Cell-Level Noise

- Why? A contradiction:

/monɛ'dɛɾɔ/	LICENSE	*[-ATR]	CRISPEGE
a. monɛ'dɛɾɔ	+3	-3	-1
(☞) b. mɔnɛ'dɛɾɔ	+4	-4	-2
(☞) c. mone'dɛɾɔ	+2	-2	

- To be less harmonic than [mɔnɛ'dɛɾɔ]:
 $w(\text{LICENSE}) > w(*[-\text{ATR}]) + w(\text{CRISPEGE})$
- To be less harmonic than [mone'dɛɾɔ]:
 $w(\text{LICENSE}) < w(*[-\text{ATR}])$
- Similarly for $*[kɔ\text{met}\epsilon\text{ɔ}]/*[kɔ\text{met}\epsilon\text{tel}\text{ɔ}]$.

Candidate- & Cell-Level Noise

Noise Type	Mean Steps	Maximum Steps
Candidate	3.09	29
Cell	3.25	23

- Consecutive steps can favor different candidates, hence slower convergence.

- Only constraint-level noise accurately models Eastern Andalusian (in all its forms).
- In this respect, serial NHG resembles parallel NHG (Kaplan 2018a; Kaplan 2019).

Revisiting Analytical Assumptions

- 1 Harmony involves a competition between LICENSE and *[-ATR]; why not use IDENT as the anti-harmony constraint?
- 2 Fell-swoop harmony vs. stepwise harmony

- Eastern Andalusian has no ATR contrast, indicating $w(*[-ATR]) > w(\text{IDENT})$, so LICENSE must compete with $*[-ATR]$.
- But using IDENT reveals interesting properties of serial NHG. . .

- In parallel NHG, the choice of *[-ATR] or IDENT is inconsequential because all vowels are [+ATR] underlyingly:¹

/rekóhelos/	*[-ATR]	IDENT(ATR)
a. re'kohelo	-1	-1
(☞) b. re'kəhelo	-2	-2
(☞) c. re'kəhelo	-3	-3
(☞) d. rɛ'kəhelo	-4	-4
e. rɛ'kəhelo	-3	-3

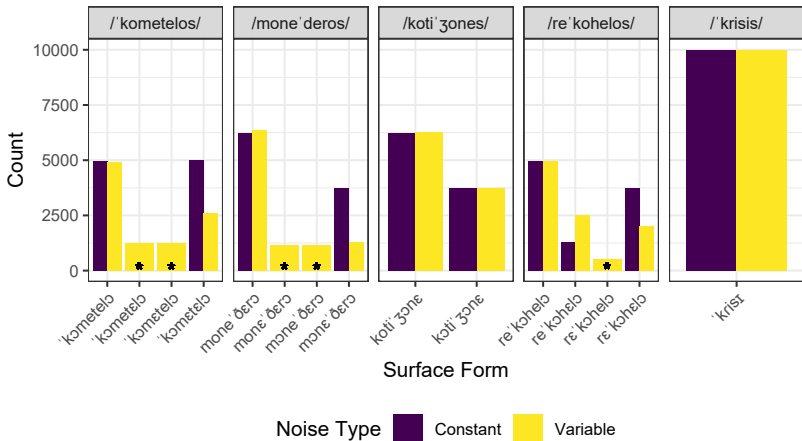
¹Setting aside rich-base inputs, of course.

- Serially, the constraints diverge: if one step creates a lax vowel, on the next step IDENT and *[-ATR] conflict.
 - Step 1: /rekóhelos/ → [re'kohelɔ]
 - Step 2:

/re'kohelɔ/	*[-ATR]	IDENT(ATR)
a. re'kohelɔ	-1	
b. re'kohelo		-1
c. re'kɔhelɔ	-2	-1
d. re'kohɛɔ	-2	-1
e. rɛ'kohelɔ	-2	-1

- On any step:
 - $w(*[-ATR]) > w(\text{LICENSE}) \rightarrow$ undo harmony (no convergence unless there's nothing to undo).
 - $w(\text{IDENT}) > w(\text{LICENSE}) \rightarrow$ stop right here (convergence!).

Constraint-Level Noise with Ident

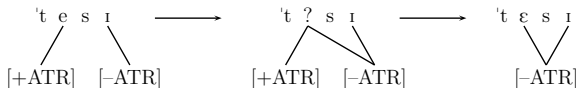


- Constant noise: either LICENSE gives maximal harmony, or IDENT gives minimal harmony.
- Variable noise: harmony proceeds until either all vowels are harmonized or IDENT gets the upper hand.

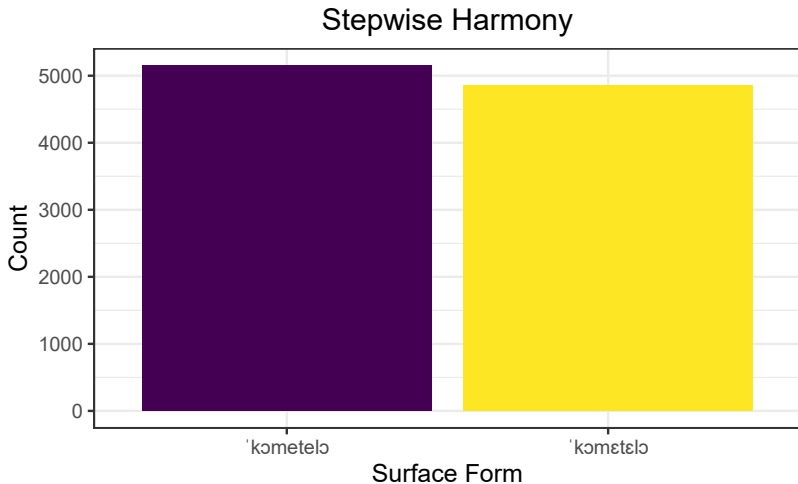
- This replicates Kimper (2011b): in Serial Variation (= Harmonic Serialism whose ranking can change on each step):
 - Markedness vs. markedness → lockstep/global optionality
 - Markedness vs. faithfulness → local optionality
- Prediction (not, I believe, noted by Kimper):
 - Local optionality occurs with contrastive features (because that implies $\text{FAITH}(F) \gg *F$, making $\text{FAITH}(F)$ the constraint participating in a variable ranking).
 - Lockstep optionality occurs with non-contrastive features (because that implies $*F \gg \text{FAITH}(F)$).
- Eastern Andalusian bears this out: lockstep harmony within the pretonic and post-tonic domains, and [ATR] is not contrastive.

- Independent evidence suggests *[-ATR] is the active constraint, not IDENT, but:
 - Constraint-level constant noise still gives good results with IDENT (until we consider rich-base inputs).
 - Using IDENT reveals that at least one version of serial NHG closely resembles Serial Variation.

Stepwise Harmony



- Potential pitfall: weights trigger the first change (spreading) but not the second change (deletion of [+ATR]) on the next step. Can we avoid convergence on *['t?si]?
- Yes: weight the constraint responsible for second step high enough so it's unlikely to be crucially dominated.
 - I.e. $w(*\text{DOUBLEASSOCIATION}) > w(\text{IDENT})$
 - *DOUBLEASSOCIATION: -1 for each segment bearing two instances of one feature.



- Only /'kometelos/ used here to keep things simple.

- Weights giving this result:

Constraint	weight
*DOUBLE	8
IDENT	1
*[-ATR]	8
LICENSE	17
MAX(-ATR)	50
ANCHOR	50

- Serial NHG is broadly similar to related frameworks:
 - Like parallel NHG, constraint-level noise models Eastern Andalusian, but candidate- and cell-noise do not.
 - With variable noise, the choice between markedness and faithfulness resembles Serial Variation.
- As far as Eastern Andalusian is concerned, constant and variable (cumulative or not) noise are roughly comparable.
- Stepwise harmony is compatible with serial NHG.
- Maybe we can draw reasonable conclusions about serial NHG from work done in parallel NHG.

Conclusion

Remaining issues

- MaxEnt (Goldwater & Johnson 2003)?
- The simulations shown here use only premultiplicative noise: add noise to weight, then multiply by violations. What about post-multiplicative noise?
- Do these conclusions hold beyond Eastern Andalusian?

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